Nonlinear Control Based on Fuzzy Logic for a Wind Energy Conversion System Connected to the Grid

L. BENAAOUINATE*‡, M. KHAFALLAH*, D. VOYER**, A. MESBAHI*, T. Bouragba***

*Laboratory of Energy & Electrical Systems (LESE), Superior National School of Electricity and Mechanical (ENSEM), Hassan II University of Casablanca-20470, Casablanca- Morocco
**Industrial systems engineering school (EIGSI), La Rochelle, France
***Industrial systems engineering school (EIGSI), Casablanca- Morocco

(l.benaaouinate@ieee.org, m.khafallah@gmail.com, voyer@eigsi.fr, abdelouahed.mesbahi@gmail.com, tarik.bouragba@eigsi.cma)

‡ Corresponding Author; L. BENAAOUINATE, 24000, Tel: +212610844961,
l.benaaouinate@ieee.org

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Abstract- This paper presents, analysis, and simulation of a variable-speed wind turbine control. Wind turbine emulator (WTE) based on induction motor (IM) is used to provide a controlled environment for testing the wind energy conversion system (WECS) control. The permanent magnet synchronous generator (PMSG) is driven by the WTE, and it is tied to the grid via back-to-back converters. The aim of the study is threefold: the development of the WTE, extracting the maximum power, and feeding captured power to the grid. However, the methods of maximum power point tracking (MPPT) using Fuzzy logic is used to maximize the wind power captured at different wind speeds. The grid-tied inverter controlled by the fuzzy adaptative PI controller is used for transferring energy to the grid and maintaining DC-Link voltage constant. Simulation results performed on the Matlab/Simulink environment verify the performance of the proposed control strategies applied on WECS tied to the grid. The used approach overcomes the non-linearity constraint of the DC-Link voltage by using a fuzzy adaptative PI controller instead of the classical PI controller. It also provides an optimal energy gain from the MPPT block based on fuzzy logic.

Keywords Wind turbine emulator (WTE), Field oriented control (FOC), Maximum power point tracking (MPPT), Voltage oriented control (VOC), Fuzzy Logic.

1. Introduction

Factors such as worrying world climate changes resulting from pollution problems, advanced power control, and economic benefits are given considerable attention to wind power as energy sources [1]. Wind Energy Conversion System (WECS) can be categorized into a fixed-speed type and a variable-speed type. As the naming indicates, fixed-speed generators rotate at practically a constant speed and directly connected to the electrical grid. Thus, the turbulence of the wind engenders strongly fluctuating power in the
WECS. Robust mechanical design is required to absorb the high mechanical stresses of this type of turbine [2,3].

However, for variable-speed WECS, the generator adjusts its rotational speed continuously according to the wind speed thanks to the power converters interface provided in its configuration. Thus, variable-speed WECS put forward several benefits, such as the operation at optimal speed using maximum power point tracking MPPT algorithm, the transfer of captured power to the grid, maximum power achieved at different wind speeds, and better efficiency. Therefore, this configuration is turning into the most commercial and the more growth application of wind energy technology [4-7].

In regards to the generators exploited in WECS, PMSG, and doubly-fed induction generator (DFIG) are the most generators used in (WECS) [8,9]. PMSG is becoming more and more commonly used thanks to its robustness, the advantage of no requirement of the gearbox by dint of the very high torque reached at low wind speeds, no notable losses are produced in the rotor system, and no need to the external excitation current. Thus, the performance of the WECS consist of PMSG has been evaluated greater than other configurations, especially for variable-speed wind turbines connected to the electrical grid [10,11].

The back-to-back converters are provided between the generator PMSG terminal and the grid control the PMSG for maximizing the captured power at different wind speed at the generator side. They control and deliver the active and reactive power into the grid by keeping the DC-Link voltage constant at the inverter input.

In the literature, several schemes have been proposed to control the various elements of the wind energy conversion system [12-14]. They consist of back-to-back converters controlled by vector control based on the conventional proportional-integral (PI) controller. These approaches present a limitation i.e., the conventional PI controller could not perform accurately with the nonlinearity of some subsystems in the WECS, especially the DC-link voltage system.

A nonlinear approach based on fuzzy logic control is applied to develop an MPPT algorithm without using characteristic data provided by the manufacturer for a given wind turbine to maximize the energy extracted from the wind generator, and to control the grid-tied inverter for DC-Link voltage regulation substituting the proportional-Integral (PI) controller to keep the DC-Link voltage constant.

This paper is structured as listed below: The design of the wind turbine emulator (WTE) based on an induction motor (IM) controlled by field-oriented control (FOC) to reproduce the dynamic behavior of a real wind turbine is detailed in section 2; The development of extracting the maximum power point MPPT algorithm based on fuzzy logic is presented in section 3; The control of PMSG and the control of the grid-tied inverter using voltage-oriented control (VOC) are provided in sections 4 and 5 respectively; The simulation results are discussed in Section 6.

2. Wind turbine emulation

Figure 1 depicts the design of the proposed WECS connected to the grid via a full-capacity back-back converters system. The PMSG is driven by a wind turbine emulator WTE based on an induction motor to substitute the real wind turbine and to provide a testing environment for WECS control strategies in a controlled and safe environment.

With the use of the power converter, the PMSG is fully decoupled from the grid and can operate in full speed range. This also enables the system to perform reactive power compensation and smooth the grid connection.

2.1. Wind turbine modelling

The wind turbine cannot wholly capture the wind power available. So, the power extracted may be expressed as [15,16].

$$P_m = \frac{1}{2} C_p(\lambda, \beta) \rho \pi R^2 v^3$$

Where \( \rho \) represents the air density (usually 1.2251 kg/m³), \( R \) represents the radius of the area swept by the wind in (m), \( C_p \) represents the power coefficient, and \( v \) represents the wind speed in (m/s) and \( \lambda \) is the tip-speed ratio (TSR).
The power coefficient $C_p$ depends on the TSR $\lambda$, which is expressed as:

$$\lambda = \frac{R \omega_m}{\nu}$$  \hspace{1cm} (2)

Where $\omega_m$ is the angular speed of the rotor in (rad/s).

The coefficient $C_p$ can be obtained by wind tunnel or simulation. It is in the form of a nonlinear function of $\lambda$ and $\beta$. Heier [17] suggests a more complex expression:

$$C_p(\lambda, \beta) = 0.5109(115.1 - 0.4\beta - 5) e^{-\frac{\lambda}{0.0065}}$$  \hspace{1cm} (3)

Moreover, the power coefficient is a nonlinear function of the blade pitch angle $\beta$ (in degrees) and the TSR $\lambda$. It achieves the maximum at the particular value of $\lambda$ called by $\lambda_{opt}$. Thus, in order to maximize the captured power by a wind turbine, $\lambda$ must be maintained at $\lambda_{opt}$.

2.2. Wind turbine emulator development

Figure 2 represents the structure of the WTE using an IM controlled by the field-oriented control system. The mathematical model of the wind turbine is developed using equation 1. The torque in the output of the mathematical model depends on the wind velocity with a stochastic profile, and it is then used as a reference in the field-oriented control system. This control system consists of controlling the stator currents of the induction motor by generating pulses to the inverter, and producing a torque depends on the wind velocity similarly required by the electrical generator as the real wind turbine.

The FOC system used to drive the induction motor is based on the identification of the stator currents as two orthogonal components generally related to the rotating magnetic field. One component defines the torque and the other the flux. Which makes the torque of IM proportional to the current and the flux, and it becomes indeed similar to that of DC motor [18].

The torque of the induction motor is defined as:

$$T_e = \frac{3}{2} p \frac{M_{sr}}{L_r} (\phi_{rd} I_{sq} - \phi_{rq} I_{sd})$$  \hspace{1cm} (5)

With $p$ is pole pairs, $M_{sr}$ and $L_r$ are the mutual inductances, $\phi_{rd}$ and $\phi_{rq}$ are the rotor flux in the dq frame, $I_{sa}$ and $I_{sq}$ are the stator currents in the dq frame.

The speed is expressed as:

$$\omega_s = p\Omega + \omega_R$$  \hspace{1cm} (6)

The expression of torque as a function of the rotor flux is given equation (5). With the FOC, we impose to orient the rotor flow along with the axis $d$, in other words, we cancel the component $\phi_{rq}$. Under these conditions, the torque is reduced to the following expression:

$$T_e = \frac{3}{2} p \frac{M_{sr}}{L_r} \phi_{rd} I_{sq}$$  \hspace{1cm} (7)

$$\omega_r = \frac{M_{sr}}{1} \frac{1}{\tau} I_{sq}$$  \hspace{1cm} (8)

Once the current setpoints have been returned to the abc reference, the hysteresis control technique is implemented. The bang-bang type hysteresis control principle is based on the comparison of sinusoidal reference currents ($isa^*$, $isb^*$, $isc^*$) with the respectively measured phase currents of the machine ($isa$, $isb$, $isc$).

Figure 3 represents the structure of the FOC used to control the IM. In this work, the FOC is applied to drive the IM by a tow-level inverter controlled by hysteresis currents control. Rotor speed $\Omega$ and stator currents are measured to define the stator pulsation $\omega_s$ and the angle of Park $\theta_s$.
3. MPPT algorithm based on fuzzy logic

The primary purpose of an MPPT algorithm is to derive the maximum power for specified wind velocity and load by generating a reference speed that corresponds to the optimal power of the wind energy conversion system [19-20].

The structure with a 3-phase PWM rectifier such as figure 1 ensures a dynamic and a reliable control in speed or torque of the PMSG generator, which provides a smooth movement of the operating point over the entire range of rotation and thereby perform research for the desired maximum power without the knowledge of the turbine characteristics curve $C_p(\lambda)$.

In the absence of any knowledge of the turbine characteristics, rules of behavior to be held to converge towards the optimal point are fairly easy to develop. These rules are based on the variations of power and speed. For example, “if I measure a power increase following a positive speed increment, I must continue to increase the speed.” From these language rules, an MPPT based on the fuzzy sets is used.

The MPPT algorithm based on the variation of DC bus power ($\Delta P$) and rotation speed ($\Delta \Omega$) generates a reference rotation speed $\Omega_{\text{ref}}$ according to the following equations:

$$\Delta P = P[k] - P[k-1]$$

$$\Delta \Omega = \Omega[k] - \Omega[k-1]$$

$$\Omega_{\text{ref}}[k] = \Omega[k-1] + \Delta \Omega_{\text{ref}}[k]$$

The major drawback of this method, based on absolute variations of power and speed, is that the variations of speed and power do not have the same weight depending on the operating point of the WECS, i.e., depending on whether the wind velocity is very high or low. The system reacts correctly only in a restricted band of wind speed according to the settings of the MPPT algorithm. Outside this area, it is difficult to adjust the dynamics of the system properly. For this reason, the input/output variables are defined as relative values. These variations are treated with the averages of the quantities measured. Equations (10), (11), and (12) describe this technique.

$$\Delta P = \frac{P[k] - P[k-1]}{P[k] + P[k-1]}$$

### Table 1. MPPT output evolution

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<th>$\frac{d\Omega}{dt}$</th>
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<td>$&lt; 0$</td>
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</table>
ΔΩ = 2 \frac{Ω[k] - Ω[k-1]}{Ω[k] + Ω[k-1]} \quad (11)

Ω_{ref}[k] = Ω[k-1] \frac{2 + ΔΩ_{ref}[k]}{2 - ΔΩ_{ref}[k]} \quad (12)

The theory of fuzzy sets is based on the concept of partial membership. Each element belongs progressively to the membership functions (fuzzy sets) a priori identified. Several membership functions can be defined on the same variable: in the case of figure 4, the variable ΔP always belongs to two membership functions.

Figure 5 presents the block diagram of a fuzzy logic stages. The Fuzzification is the first stage of the fuzzy logic process; it converts the input data into the fuzzy representation using membership functions. The inference is the second stage of the process; it evaluates the rules and generates results using output membership functions. The De-Fuzzification is the third and last stage of the process; it translates the membership functions to a numerical value for Ω_{ref}[k].

**Fig. 5.** block diagram of a fuzzy logic stages.

The Fuzzification operation provides a transformation from the real domain to the fuzzy domain. It determines the degree of membership (μ) of an input variable for a given membership function. The degree of membership represents the degree of truth of the membership function.

**Table 2.** Rules Base for Fuzzy Logic

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The abbreviations used in Table 2 are given by:

HN: Huge Negative; AN: Average Negative; lN: little negative; Z: Zero; HP: Huge Positive; AP: Average Positive; IP: little Positive.

In our case, the center of gravity (COG) approach is used in the De-Fuzzification. This method is based on the sum of the centers of gravity of each sub-area of the total area of the membership function distribution.

The defuzzified value \( x_0 \) using COG is expressed as:

\[
x_0 = \frac{\sum_{i=1}^{n} \mu_c(x_i)}{\sum_{i=1}^{n} \mu_c(x_i)}
\]  

(13)

With \( x_i \) is the sample element \( \mu_c(x_i) \) is the membership function, and \( n \) represents the number of the sample element.

4. **PMSG control system**

In the dq synchronous frame, the stator voltages of the PMSG are expressed as [21-22]:

\[
\begin{align*}
v_{ds} &= -R_s i_{ds} - L_d \frac{di_{ds}}{dt} + \omega L_q i_{qs} \\
v_{qs} &= -R_s i_{qs} - L_q \frac{di_{qs}}{dt} + \omega \Phi_f
\end{align*}
\]

(14)

Where \( R_s \) is stator resistance \( i_{sd}, i_{sq} \) are d-q axis stator current, \( L_d \) and \( L_q \) are d-q axis inductance, \( \omega \) is pulsation and \( \Phi_f \): flux.

The torque is defined by [23]:

\[
T_{em} = \frac{3}{2} p [(L_q - L_d) i_{ds} i_{qs} + i_{qs} \Phi_f]
\]

(15)

Where \( p \) designates the number of poles pairs.

According to the principle of FOC, the electromagnetic torque depends only on the q-axis current component; we obtain then:

\[
T_{em} = \frac{3}{2} p i_{qs} \Phi_f = K \cdot i_{qs}
\]

(16)

The dynamic of the PMSG rotor can be expressed as:

\[
\frac{d\omega}{dt} = \frac{T_m - T_e - B \omega}{J}
\]

(17)

With \( J \) is the total inertia (kg m²), \( B \) is viscous friction coefficient (kg m²/s), and \( T_m \) is the drive torque produced by wind turbine emulator.

According to equation (16), the PMSG speed can be controlled by the q-axis current component. As presented in figure 6, the reference speed from the MPPT device is used to generate the reference torque, and then the q-axis current component. The d-axis current component is set to zero.
5. Control of grid-connected inverter

5.1. Voltage Oriented Control

The literature on the control of grid-connected inverter shows a variety of approaches. Such one is known as voltage-oriented control (VOC), as shown in figure 7. For the implementation of the VOC scheme, the grid voltages are measured to estimate the phase angle \( \theta_g \) using phase-locked loop (PLL). The variables are transformed from the abc stationary form to the dq synchronous form, and vice versa using the grid voltage angle \( \theta_g \) [24-26].

Figure 7 shows a VOC system scheme.

The VOC system consists of three feedback control loops: one external feedback loop to regulate the DC-Link voltage, and two internal dq-axis currents loops. The active and reactive components of the grid currents \( i_{ag}, i_{bg}, \) and \( i_{cg} \) are \( i_{dg} \) and \( i_{qg} \), respectively. These two components are controlled independently, which provide independent control of active and reactive power system.

The active and reactive powers are expressed as [27-28]:

\[
\begin{align*}
    P_a &= \frac{3}{2} (V_{ag} i_{ag} + V_{bg} i_{bg}) - \frac{3}{2} V_{dg} i_{dg} \\
    Q_a &= \frac{3}{2} (V_{ag} i_{ag} - V_{bg} i_{bg}) - \frac{3}{2} V_{dg} i_{dg}
\end{align*}
\]  

(18)

With \( V_{qg} = 0 \), since the VOC scheme aligns the grid voltage with the \( d \)-axis of the synchronous frame, i.e. \( V_{dg} = V_d \).

The transformation abc/dq or vice versa in our work preserves the amplitudes of voltages and currents.

According to equation (18), the setpoint of q-axis current \( i_{qg}^* \) is expressed as:

\[
    i_{qg}^* = -\frac{Q_g^*}{1.5 V_d}
\]

(19)

Where \( Q_g^* \) represents the setpoint of reactive power.

The setpoint of the active power of the system is represented by the setpoint of \( d \)-axis current \( i_{dg}^* \) generated by the fuzzy adaptive PI controller for DC-Link voltage regulation. The DC-link voltage remains constant at a reference value \( V_{dc}^* \).

The equation that describes the DC-Link voltage system is as follows [29-35]:

\[
    C \frac{dV_{dc}}{dt} = \frac{3}{2} V_{ag} i_{ag} - i_{ag}
\]

(20)

With \( C \) represents the DC-Link capacity, \( V_{dc} \) represents the DC-link voltage.
5.2. Fuzzy adaptive PI controller

According to equation (20), the DC-Link system is nonlinear. Thus, the control of the external feedback loop of the DC-Link voltage could not perform accurately with linear control approaches. To overcome this issue, it is necessary to adopt a nonlinear approach, such as fuzzy logic control. It is presented in this work to substitute the Proportional-Integral PI controller.

In this work, a fuzzy adaptive PI controller is proposed, as presented in Figure 8. This type of control, called adaptive, allows exploiting the advantages presented by the PI controller and those of the fuzzy logic. The purpose of the adaptation law is to improve the control performance of complex and nonlinear systems.

The fuzzy adaptive PI controller changes its gain constant according to the error (e) between the setpoint value of the DC-link voltage and its measured value and the variation of error (Δe)[33]:

\[
\begin{align*}
\varepsilon &= V_{dc}^* - V_{dc} \\
\Delta e &= e(t) - e(t - \Delta t)
\end{align*}
\]  (21)

The FLC generates the normalized signals ΔKP and ΔKI used to compute the gain of the PI controller:

\[
\begin{align*}
K_p &= K_{p0} + G_p \Delta K_p(e, \Delta e) \\
K_i &= K_{i0} + G_i \Delta K_i(e, \Delta e)
\end{align*}
\]  (22)

Where Kp represents the proportional gain, and Ki represents the integral gain. Kp0 and Ki0 are the two control parameters in the initial state; they are estimated using Ziegler and Nichols method. The values of the gains Gp and Gi are introduced since ΔKp1 and ΔKi1 are normalized quantities defined in the interval [-1, 1].

![Fig. 8. Fuzzy adaptive PI for the control of the DC-link voltage.](image)

The fuzzy system is used to modify in real-time the PI parameters according to the behavior of the process. Basically, Kp provides a fast-dynamic response while Ki eliminates the static error and ensures the stability of the system. When the error is large, Kp should be large and Ki small; when the error is small, Kp should be small and Ki large. Thus, specific rules in the fuzzy process can be built matrix to optimize the characteristics of the temporal response. The rule base chosen in this paper is reported in Table 3.

**Table 3. Fuzzy logic rules.**

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The abbreviations are defined as follows: HN is Huge Negative, N is Negative, IN is little Negative, ZE is Zero, HP is Huge Positive, P is positive, and IP is little Positive.

The logic for determining this matrix of rules is based on global or qualitative knowledge of how the system works. Indeed, it is completely normal to increase Kp and decrease Ki. When the error is large; when the error is small, Kp should be small and Ki large. Table 3 summarizes all the rules of human know-how, it translates the rules expressed by the following common language:

- When the error e and its variation Δe are large negatives (HN), ΔKp should be greatly decreased (HN) and ΔKi greatly increased (HP).
- When the error e and its variation Δe are small negatives (IN), ΔKp should be greatly decreased (HN) and ΔKi greatly increased (HP).

6. Simulation and analysis

The complete WECS is simulated using the different models and control strategies presented in previous sections. The block diagram, integrating these various elements and forming the whole structure of a wind system, is given in figure 9.

The block of the induction motor model is controlled by a 2-level inverter using a FOC strategy to generate a mechanical torque depends on wind speed and different proprieties of the wind turbine for substituting the real wind turbine and to provide a testing environment for WECS control strategies in a controlled and safe environment. The PMSG is driven by the induction motor and controlled by a rectifier to maximize the maximizing captured power at different wind speeds. The inverter in
the grid side ensures the control and deliver the active and reactive power into the grid by keeping the DC-Link voltage constant.

Fig. 9. The entire structure of the wind system.

6.1. Emulation Results:

Fig. 10. Wind speed profile.

Fig. 11. Speed of Induction Motor.

Fig. 12. The torque of Induction Motor.

Fig. 13. Power coefficient $C_p$ versus TSR $\lambda$.

Figures 11 and 12 represent the speed and the torque of the WTE, respectively. The variations of these correspond to the wind speed profile (figure 10) applied to the wind turbine model. The non-dimensional curve of power coefficient $C_p$ versus TSR $\lambda$ characterize the wind turbine $C_p(\lambda)$ is represented in figure 13. For the optimum TSR (when $\lambda = 8$), the power coefficient is at maximum, and the wind turbine delivers the maximum of mechanical power.

The torque shown in Figure 12 corresponds to the reference torque from the wind turbine model, except for the moments at start where the reference torque is too high (the torque ordered has been limited for safety reasons).

The curve of the power coefficient $C_p$ versus the TSR Tip Speed Ratio $\lambda$. $C_p(\lambda)$ characterizes the wind turbine, and it can be used to achieve MPPT (Maximum Power Point Tracking) for an Optimal TSR ($\lambda = 8$) the power coefficient $C_p$ is maximum.

6.2. MPPT Results:

Fig. 14. Mechanical speed and optimal speed of PMSG.
Figure 14 shows the mechanical speed of PMSG optimized by the fuzzy MPPT compared to the curve of the optimal rotation speed calculated according to equation (23):

$$\Omega_{opt} = \frac{\lambda_{opt} \cdot v}{R}$$

(23)

The mechanical speed of PMSG determines the operating point relative to the maximum powerpoint. The difference between the MPPT speed and the optimal speed is then reflected in a power loss shown in figure 15. The optimal power curve calculated using expression (24):

$$P_{opt} = \frac{1}{2} \cdot C_{p}^{opt} \cdot \rho \cdot S \cdot u^3$$

(24)

Figure 16 represents the efficiency of the system calculated according to equation (25):

As can be depicted in figure 16 the algorithm is reliable with an efficiency of 88%.

When the wind energy conversion system operates under MPPT control, the power coefficient $C_p$ of the wind turbine is maintained to its maximum value ($C_{p_{max}}=0.48$), as it can be depicted in figure 17.

The difference between the optimal energy and that from the MPPT device gives a quantified overview of the quality of the energy extraction over a given period and a representation of the energy "captured" by the system, which is a relevant criterion of appreciation of energy efficiency.

The difference calculated using equation (28):
The total energy optimized by MPPT device and the maximum energy which can be extracted from a given wind profile during the test time (figure 18) delivers a difference of 4.07%. However, this energy difference is worth 39.6% (figure 19) for an equivalent system, but operating at a constant speed, i.e., without MPPT device. Which allows an energy gain offered by the MPPT device of 35.5%.

6.3. Grid-connected system results

![Figure 20. DC-Link Voltage.](image)

Figure 20 presents the measured DC-Link voltage controlled by a Fuzzy adaptive PI controller, where it reveals nearly no voltage fluctuation, with a steady-state error equal 2V, which represents 0.29% of the reference voltage value 700V.

![Figure 21. Active Power.](image)

The active and reactive powers of the grid are presented in figure 21 and figure 22, respectively. As mentioned above, the active and reactive powers are controlled independently. The active power is stabilized, and the reactive power equals zero, which corresponds to operation with a unity power factor.

![Figure 22. Reactive Power.](image)

The currents injected to the electrical grid results are shown in Figure 23. To investigate the quality of the power injected to the grid, the fundamental and harmonic

![Figure 23. Currents injected into the grid.](image)

![Figure 24. Signal and Fast Fourier Transform FFT analysis of the current signal.](image)

The currents injected to the electrical grid results are shown in Figure 23. To investigate the quality of the power injected to the grid, the fundamental and harmonic
components in the current injected to the grid signal are extracted using the Powergui FFT Analysis Tool in MATLAB. As it can be illustrated in figure 24, the fundamental current supplied to the grid equals 4.78A, and the total harmonic distortion THD is 1.21 %.

7. Conclusion

This work deals with a nonlinear control approach of the variable-speed WECS consists of the PMSG connected to the electrical grid through back-to-back converters.

The fuzzy logic approach is used to implement the (MPPT) and DC bus voltage regulation. The nonlinear control strategy based on the fuzzy logic suggested in this work can overcome the non-linearity of the DC-Link voltage system and ensure a dynamic and reliable control of the PMSG with desired maximum power without the knowledge of the turbine characteristics curve $C_p(\lambda)$.

An experimental evaluation of the simulation results will be treated as the future scope of this work.

Appendix

Table 4. Parameters of the proposed WECS

<table>
<thead>
<tr>
<th>Parameters of the wind turbine model</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\rho$ the air density</td>
<td>1.225 kg/m$^3$</td>
</tr>
<tr>
<td>$R$ the radius of the blades</td>
<td>2.5 m</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Parameters of Induction motor</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pr rated power</td>
<td>3kW</td>
</tr>
<tr>
<td>om rated mechanical speed</td>
<td>1430 rpm</td>
</tr>
<tr>
<td>Rs stator resistance</td>
<td>2.3 $\Omega$</td>
</tr>
<tr>
<td>$L_s$ stator $d$-axis inductance</td>
<td>163mH</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Parameters of the PMSG</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stator resistance $Rs(\Omega)$</td>
<td>1.137</td>
</tr>
<tr>
<td>Stator $d$-axis inductance $L_d$</td>
<td>2.7 mH</td>
</tr>
<tr>
<td>Stator $q$-axis inductance $L_q$</td>
<td>2.7 mH</td>
</tr>
<tr>
<td>Flux $\Phi$ (Wb)</td>
<td>0.15</td>
</tr>
<tr>
<td>$P$ poles pairs number</td>
<td>17</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Parameters of the grid side</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$V_{dc}$ DC-Link Voltage reference (V)</td>
<td>700V</td>
</tr>
<tr>
<td>C DC-Link capacitor (mF)</td>
<td>50</td>
</tr>
<tr>
<td>$L$ Filter resistance ($\Omega$)</td>
<td>0.5</td>
</tr>
<tr>
<td>$L$ Filter inductance (mH)</td>
<td>25</td>
</tr>
</tbody>
</table>

References


[22] Shenuqin Li, Kezhao zhang, Juan Li, Chao liu, ‘ On the rejection of internal and external disturbances in a wind energy conversion system with direct-driven PMSG’, ISA Transactions, 2016, 61 , pp. 95-103.


